

Bell work: Expand the following binomials

$$1) (x+2)^2$$

$$(x+2)(x+2)$$

$$x^2 + 2x + 2x + 4$$

$$x^2 + 4x + 4$$

$$2) (x-y)^2$$

$$(x-y)(x-y)$$

$$x^2 - xy - xy + y^2$$

$$x^2 - 2xy + y^2$$

$$(x-y)^3$$

$$(x-y)(x-y)(x-y)$$

Pascal's Triangle

$(a+b)^0$	1	1	1	1	1	1	1	1	1	1
$(a+b)^1$		1	2	1						
$(a+b)^2$			1	3	3	1				
$(a+b)^3$				1	4	6	4	1		
$(a+b)^4$					1	5	10	10	5	1
						1	6	15	20	15
							7	21	35	35
								8	56	70
									28	56
										28
										8

Expand each binomial.

1. $(x+4)^3$ *4 terms*

$$\begin{aligned} & (x)^3 + (x)^2(4)^1 + (x)^1(4)^2 + (4)^3 \\ & \cancel{x^3} + \cancel{4x^2} + \cancel{16x} + \cancel{64} \\ & x^3 + 12x^2 + 48x + 64 \end{aligned}$$

$$\begin{array}{ccccccccc} & & & & & 1 & & & \\ & & & & & | & & & \\ & & & & & 1 & & & \\ & & & & & | & & & \\ & & & & & 1 & 2 & & \\ & & & & & | & | & & \\ & & & & & 1 & 3 & 3 & 1 \\ & & & & & | & | & & \\ & & & & & 1 & 4 & 6 & 4 \\ & & & & & | & | & & \\ & & & & & 1 & 5 & 10 & 10 & 5 \\ & & & & & | & | & & \\ & & & & & 1 & 6 & 15 & 20 & 15 & 6 \\ & & & & & | & & & \\ & & & & & 1 & & & \end{array}$$

3. $(x-3)^5$

$$\begin{aligned} & (x)^5 + (x)^4(-3)^1 + (x)^3(-3)^2 + (x)^2(-3)^3 + (x)^1(-3)^4 + (-3)^5 \\ & \cancel{x^5} + \cancel{-3x^4} + \cancel{9x^3} - \cancel{27x^2} + \cancel{81x} - \cancel{243} \\ & x^5 - 15x^4 + 90x^3 - 270x^2 + 405x - 243 \end{aligned}$$

Find the specified term of each binomial expansion.

5. second term of $(x - 4)^8$ - 9 terms

$$(x)^8 + (x)^7(-4)^1 \\ x^8 - 4x^7 (8) \\ x^8 \cancel{- 32x^7}$$

7. fourth term of $(x - 2)^7$ - 8 terms

$$(x)^7 + (x)^6(-2)^1 + (x)^5(-2)^2 + (x)^4(-2)^3 \\ (1) x^7 - \frac{1}{2}x^6 + 4x^5 \cancel{- 8x^4} (35) \quad x^7 - 14x^6 + 84x^5 \cancel{- 280x^4}$$

State the number of terms in each expansion and give the first two terms.

9. $(2a + b)^7$

$$(2a)^7 + (2a)^6(b)^1$$

$$(1) 128a^7 + \frac{7}{6}4a^6b$$

$$128a^7 + 448a^6b$$

13. $(x + y^2)^5$

$$(x)^5 + (x)^4(y^2)^1$$

$$(1) x^5 + x^4 y^2$$

$$x^5 + 5x^4 y^2$$

11. $(x + y)^6$

$$(x)^3 + (x)^2(y)^1$$

- 4 terms

$$(1) x^3 + x^2 y^3$$

$$x^3 + 3x^2 y$$

Expand each binomial.

21. $(3b + 1)^6$ *- 7 terms*

$$\begin{aligned} & (3b)^6 + (3b)^5(1)^1 + (3b)^4(1)^2 + (3b)^3(1)^3 + (3b)^2(1)^4 + (3b)^1(1)^5 + 1^6 \\ & \frac{1}{1} \cdot 29b^6 + \frac{6}{1} \cdot 3b^5 + \frac{15}{1} \cdot b^4 + \frac{20}{1} \cdot b^3 + \frac{15}{1} \cdot b^2 + \frac{6}{1} \cdot b + 1 \\ & 729b^6 + 1458b^5 + 1215b^4 + 540b^3 + 135b^2 + 18b + 1 \end{aligned}$$

17. $(2y + 8)^3$ *- 4 terms*

$$\begin{aligned} & (2y)^3 + (2y)^2(8)^1 + (2y)^1(8)^2 + (8)^3 \\ & 8y^3 + 4y^2(8) + 2y(64) + 512 \\ & (1)8y^3 + \frac{3}{1}2y^2 + \frac{3}{1}8y + 512 \quad 8y^3 + 96y^2 + 384y + 512 \end{aligned}$$

