

Section 3 – Topic 3
Graphing and Writing
Piecewise-Defined Functions – Part 1

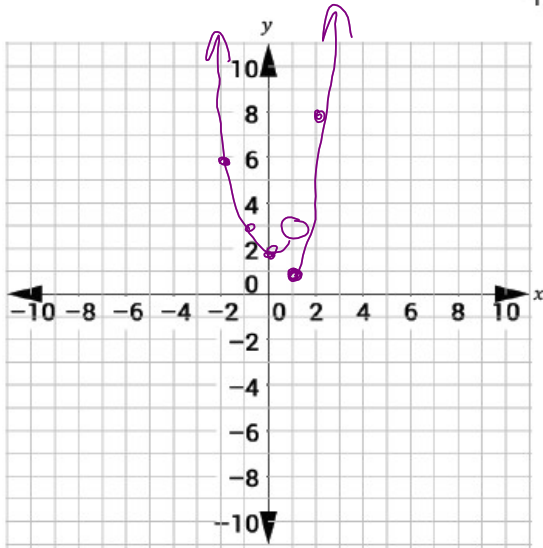
To graph piecewise-defined functions, graph each “piece” of the function on the same graph.

Domain restrictions must be considered when graphing each piece.

Domain - x-values

Let's Practice!

- Graph the following piecewise-defined function.



$$f(x) = \begin{cases} x^2 + 2, & x < 1 \\ x^3, & x \geq 1 \end{cases}$$

$$x^2 + 2$$

x	y
1	3
0	2
-1	3
-2	6

$$x^3$$

x	y
1	1
2	8
3	27

a. What is the domain of the function?

$(-\infty, \infty)$

b. What is the range of the function?

$[1, \infty)$

c. What, if any, are the x -intercepts of the function?

none

d. What, if any, is the y -intercept of the function?

$y = 2$ $(0, 2)$

e. Over what interval(s) is the function increasing?
 Decreasing?

Increasing $(0, 1), (1, \infty)$

Decreasing $(\infty, 0)$

f. What, if any, are the relative maximums of the graph?

none

g. What, if any, are the relative minimums of the graph?

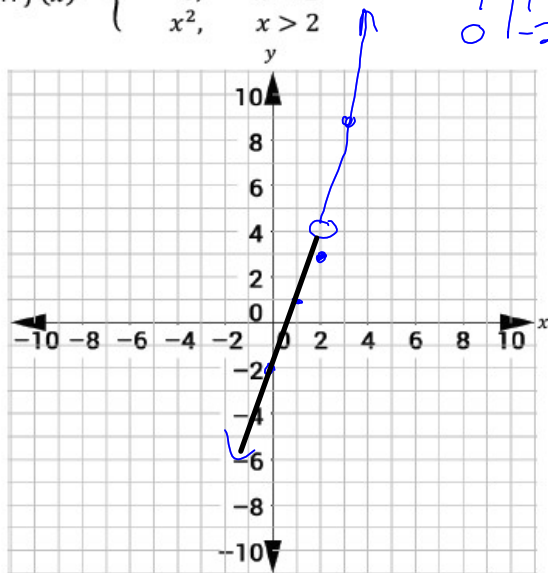
$(0, 2)$

h. Is this function considered to be continuous? Why or why not?

no, because there is a gap at $x=1$

Try It!

2. Graph $f(x) = \begin{cases} 3x - 2, & x < 2 \\ 3, & x = 2 \\ x^2, & x > 2 \end{cases}$



$$3x - 2$$

x	y
2	4
1	1
0	-2

$$x^2$$

x	y
2	4
3	9
4	16

a. What is the domain of the function?

$$(-\infty, \infty)$$

b. What is the range of the function?

$$(-\infty, 4) \cup (4, \infty)$$

c. Is the function continuous?

no

U = Union - break in the graph