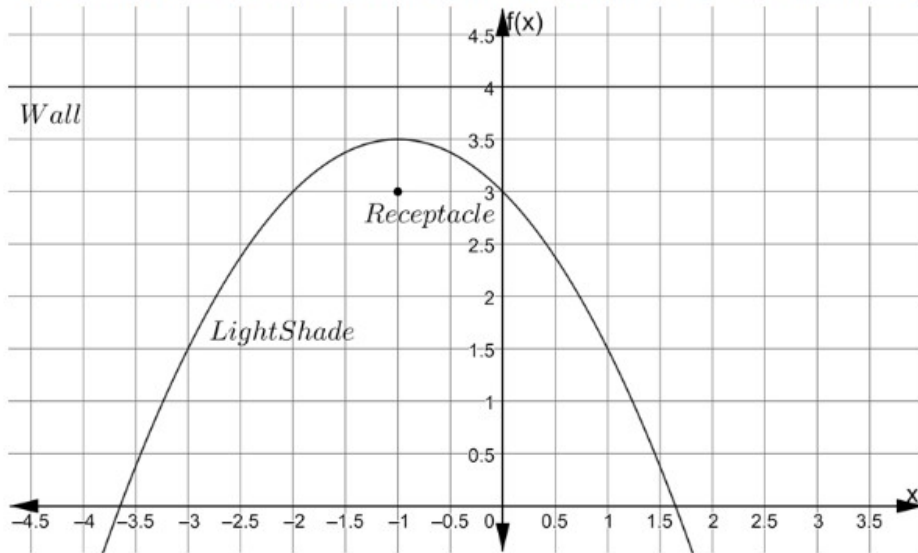


TOPIC 7: WRITING QUADRATIC EQUATIONS WHEN GIVEN A FOCUS AND DIRECTRIX - 5/7/FR



The 2-dimensional sketch of a parabolic light shade is shown. The bulb receptacle is placed at $(-1, 3)$ and the wall, which must be the same distance away from the light shade as the receptacle, is at $y = 4$. What is the equation of the quadratic that is the outline of the light shade?

Answer:

$y = \underline{-\frac{1}{2}x^2 - x + 3}$

$$\begin{aligned} \sqrt{(x+1)^2 + (y-3)^2} &= \sqrt{(y-4)^2} \\ x^2 + 2x + 1 + y^2 - 6y + 9 &= y^2 - 8y + 16 \\ x^2 + 2x + 1 - 6y + 9 &= -8y + 16 \\ x^2 + 2x + 10 - 6y &= -8y + 16 \\ -16 + 6y + 6y - 16 & \\ x^2 + 2x - 6 &= -2y \end{aligned}$$

TOPIC 7: WRITING QUADRATIC EQUATIONS WHEN GIVEN A FOCUS AND DIRECTRIX - 5/7/DD

The equation of the parabola with the focus $(-4, 1)$ and the directrix $y = -1$ is

A $\frac{x^2}{4} - 2x + 4$

B $\frac{x^2}{4} + 2x + 4$

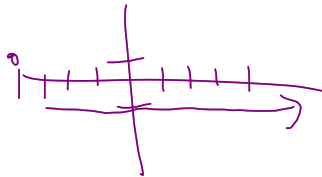
C $x^2 + 2x + 4$

and has the vertex

A $(-4, 0)$

B $(4, 0)$

C $(0, -4)$



$$\sqrt{(x+4)^2 + (y-1)^2} = \sqrt{(y+1)^2}$$

$$x^2 + 8x + 16 + y^2 - 2y + 1 = y^2 + 2y + 1$$

~~$x^2 + 8x$~~

$$x^2 + 8x + 16 - 2y = 2y + 1$$

$$-1 + 2y + 2y - 1$$

$$\frac{x^2 + 8x + 16}{4} = 4y$$

Question 3 of 8

TOPIC 8: SYSTEMS OF EQUATIONS WITH QUADRATICS - PART 1 - 5/8/FR

Consider the system.

$$f(x) = x^2 - 7x + 5$$

$$g(x) = 3x - 20$$

For what value of x is $f(x) = g(x)$?

Answer:

$$x = 5$$

$$\begin{aligned} x^2 - 7x + 5 &= 3x - 20 \\ -3x + 20 & \quad -3x + 20 \end{aligned}$$

$$x^2 - 10x + 25 = 0$$

$$\frac{10 \pm \sqrt{10^2 - 4(1)(25)}}{2(1)} = \frac{10 \pm \sqrt{100 - 100}}{2}$$
$$\frac{10}{2} = 5$$

TOPIC 9: SYSTEMS OF EQUATIONS WITH QUADRATICS-PART 2 - 5/9/DD

Janel and Fred each throw a ball. The vertical heights of the balls, in meters, after t seconds are modeled by the system below.

$$f(t) = 45 - 5(t - 3)^2$$

$$g(t) = 45 - 5(t - 1)^2$$

The balls collide at

- (A) 1
- (B) 2
- (C) 3

seconds at a height of

- (A) 45
- (B) 40
- (C) 35

meters.

$$\cancel{45 - 5(t - 3)^2} = \cancel{45 - 5(t - 1)^2}$$

$$\cancel{t^2} - 6t + 9 = \cancel{t^2} - 2t + 1$$

$$\begin{matrix} +6t & -1 \\ +6t & -1 \end{matrix}$$

$$8 = 4t$$

$$45 - 5(2 - 1)^2$$

$$45 - 5 = 40$$

TOPIC 9: SYSTEMS OF EQUATIONS WITH QUADRATICS-PART 2 - 5/9/FR

Alicia is constructing a sculpture of two glass parabolic structures joined at one point. She models the parabolas with the functions, $f(x) = (x + 3)^2 - 1$ and $g(x) = 7 - (x - 1)^2$. At what x -value are the two parabolas joined?

Answer:

$$\underline{x} = \underline{-1}$$

$$x^2 + 6x + 9 - 1 = 7 - (x^2 - 2x + 1)$$

$$x^2 + 6x + 8 = 7 - x^2 + 2x - 1$$

$$x^2 + 6x + 8 = -x^2 + 2x + 6$$

$$+ x^2 - 2x - 6$$

$$2x^2 + 4x + 2 = 0$$

$$2(x^2 + 2x + 1) = 0$$

$$\frac{-2 \pm \sqrt{2^2 - 4(1)(1)}}{2(1)} = \frac{-2}{2} = -1$$

TOPIC 12: KEY FEATURES OF QUADRATIC FUNCTIONS - 5/12/MC

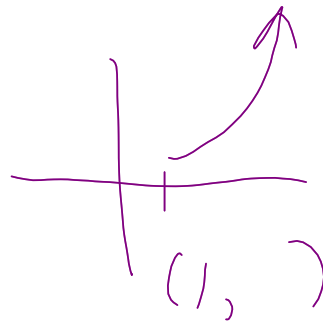
A quadratic function is increasing over the interval $(1, \infty)$. Which of the following could be the equation of the function?

A $f(x) = (x - 1)^2 - 4$

B ~~$f(x) = (x - 4)^2 + 1$~~

C $f(x) = -(x - 1)^2 - 4$

D ~~$f(x) = -(x - 4)^2 + 1$~~



TOPIC 13: CLASSIFYING QUADRATIC FUNCTIONS AND FINDING INVERSES - 5/13/MS

Two functions $f(x)$ and $g(x)$ are defined as:

$$f(x) = x^2 + 12x + 38 \text{ for } x \geq -6 \quad g(x) = \sqrt{x-2} - 6$$

Which statements are correct? Select all that apply.

$f(g(x)) = g(f(x)) = 1$

$f(g(x)) = g(f(x)) = x$

$f(x)$ and $g(x)$ are inverse functions.

For $f(x)$ and $g(x)$ to be inverses, $g(x)$ should be equivalent to $\frac{1}{f(x)}$.

For $f(x)$ and $g(x)$ to be inverses, the restriction on $f(x)$ should be $x \leq -6$.

$$\sqrt{x^2 + 12x + 38} - 2 - 6$$

$$\sqrt{x^2 + 12x + 36} - 6$$

$$\sqrt{(x+6)^2} - 6$$

$$\begin{aligned} x+6-6 \\ = x \end{aligned}$$

$$\begin{array}{r|l} 36 & 12 \\ \hline 6(6) & 6+6 \end{array}$$

